

Deduction of Gas laws from kinetic theory

(a) Boyle's law —

$$V \propto \frac{1}{P} \text{ When } T \text{ is constant}$$

$$PV = \text{Constant}$$

We have already derived with the help of kinetic theory —

$PV = \frac{2}{3}KT$ if T is constant, PV will be constant.

(b) Charles's law —

$$V \propto T, \text{ if } P \text{ is constant}$$

$$\therefore PV = \frac{2}{3}KT$$

$$\text{or } V = \left[\frac{2K}{3P} \right] T$$

Since K & P are constants

$$\therefore V \propto T$$

(c) Graham's law of diffusion: —

from kinetic equation —

$$PV = \frac{1}{3}mnc^2$$

$\therefore M = m \times n = \text{total mass of mass}$

Hence —

$$PV = \frac{1}{3} Mc^2$$

$$\text{or } c^2 = \frac{3PV}{M}$$

$$\left[\because \frac{M}{V} = D \text{ (density)} \right]$$

$$c^2 = \frac{3P}{M/V} = \frac{3P}{D} \quad \therefore c^2 \propto \frac{1}{D}, \text{ when } P \text{ is constant}$$

$$\therefore c = \sqrt{\frac{1}{D}}$$

This equation represents

Graham's law of diffusion of gas.